

# Effect of grain width and aspect ratio on mechanical properties of Si<sub>3</sub>N<sub>4</sub> ceramics

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**Abstract** Sintering additives Y<sub>2</sub>O<sub>3</sub> and Al<sub>2</sub>O<sub>3</sub> with different ratios ((Y<sub>2</sub>O<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub>) from 1 to 4) were used to sinter Si<sub>3</sub>N<sub>4</sub> to high density and to induce microstructural changes suitable for raising mechanical properties of the resultant ceramics. The sintered Si<sub>3</sub>N<sub>4</sub> ceramics have bimodal microstructures with elongated β-Si<sub>3</sub>N<sub>4</sub> grains uniformly distributed in a matrix of equiaxed or slightly elongated grains. Pores were found within the grain boundary phase at the junction regions of Si<sub>3</sub>N<sub>4</sub> grains. The highest average aspect ratio (length/width of the grains) of ~4.92 was found for Y<sub>2</sub>O<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> ratio of 2.33 with fracture toughness and strength values of ~7 MPam<sup>1/2</sup> and 800 MPa, respectively. The effect of microstructure, specifically grain morphology, on mechanical properties of sintered Si<sub>3</sub>N<sub>4</sub> were investigated and found that the aspect ratio of the elongated grains is the most important microstructural feature which controls mechanical properties of these ceramics.

## Introduction

Evolution of microstructure during sintering of Si<sub>3</sub>N<sub>4</sub> and its effect on mechanical properties has been one of the main topics of numerous studies over the last number of years [1–8]. The properties of Si<sub>3</sub>N<sub>4</sub> ceramics strongly depend on the microstructure developed during different sintering conditions, therefore microstructural design is a key factor in optimization of processing parameters and mechanical properties of Si<sub>3</sub>N<sub>4</sub> ceramics.

The amount of sintering aids used affects the density of the ceramics [9] and the chemical composition of the grain boundary phase. The chemistry of the liquid phase, formed between sintering aids and oxide layer (SiO<sub>2</sub>) on the surface of the Si<sub>3</sub>N<sub>4</sub> particles, along with characteristics of the sintering powder and processing conditions, are the key factor in determining the microstructure and mechanical properties of Si<sub>3</sub>N<sub>4</sub> ceramics [9].

Woetting and Ziegler [10] in 1984 showed that the presence of Al<sub>2</sub>O<sub>3</sub> and Y<sub>2</sub>O<sub>3</sub> has a strong effect on density and grain shape and any increase of Y<sub>2</sub>O<sub>3</sub> concentration leads to an increase in liquidus temperatures and thus to viscosities at the sintering temperature. The development of elongated β-Si<sub>3</sub>N<sub>4</sub> depends mainly on the diffusion rate during α to β phase transformation, and on the viscosity of the liquid at the sintering temperature. The higher the viscosity the lower the diffusion rates and thus the higher the aspect ratio of β-Si<sub>3</sub>N<sub>4</sub> elongated grains will be. The aspect ratio is defined as [11]

$$\begin{aligned} \text{AR} &= \frac{L}{W} = \left( \frac{K_L^{1/3}}{K_W^{1/5}} \right) \cdot t^{(1/3-1/5)} = \left( \frac{K_L^{1/3}}{K_W^{1/5}} \right) \cdot t^{(2/15)} \\ &= \left( \frac{K_{OL}^{1/3}}{K_{OW}^{2/15}} \right) \cdot t^{(2/15)} \exp \left[ \frac{\left( \frac{Q_L}{3} - \frac{Q_W}{5} \right)}{RT} \right] \end{aligned} \quad (1)$$

where  $L$  is the average length of the β-Si<sub>3</sub>N<sub>4</sub> grains,  $W$  is the average width of the β-Si<sub>3</sub>N<sub>4</sub> grains,  $K_L$  and  $K_W$  are the rate constants in the length and width direction of the β-Si<sub>3</sub>N<sub>4</sub> grains,  $Q_L$  and  $Q_W$  are the activation energies for length and width respectively,  $R$  is the gas constant,  $t$  is the time and  $T$  is the absolute temperature. Due to prismatic configuration of β-Si<sub>3</sub>N<sub>4</sub> grains, the growth of length in the  $c$  direction [0001] is controlled mainly by the solute diffusion through multigrain junctions, while the growth of

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width in the [2100] direction is controlled by the diffusion along grain boundaries. According to this, the growth rate in the width direction is lower than the growth in the length direction resulting in the formation of elongated  $\beta$ -Si<sub>3</sub>N<sub>4</sub> grains.

These elongated grains produced in the same matrix material have an important role in toughening of Si<sub>3</sub>N<sub>4</sub> ceramics. The two most important mechanisms of toughening in this self-reinforced or in situ reinforced Si<sub>3</sub>N<sub>4</sub> ceramics are crack bridging and crack deflection. In order for crack bridging to occur, the microstructure must consist of rod-like  $\beta$ -Si<sub>3</sub>N<sub>4</sub> elongated grains uniformly distributed in a matrix of smaller either slightly elongated or equiaxed grains. These two mechanisms contribute to enhanced energy dissipation upon crack propagation and hence can result in increase fracture toughness [12]. It should be noted that a weak interface between the elongated grains and surrounding intergranular phase are generally required for these two toughening mechanisms to operate. The resulting fracture toughness of monolithic Si<sub>3</sub>N<sub>4</sub> ceramics is reported in the literature to be mainly governed by the morphology of the Si<sub>3</sub>N<sub>4</sub> grains, i.e., the grain diameter and aspect ratio of the grains [12–14]. Faber and Evans [15] developed a model for toughening mechanism by crack deflection which relates fracture toughness and aspect ratio. In that model, any increase in aspect ratio of the rod shape reinforcing particles increases fracture toughness. Correlation between the square root of the average grain diameter and fracture toughness, and a linear relationship between aspect ratio of the elongated Si<sub>3</sub>N<sub>4</sub> particles and fracture toughness was observed by Mitomo and Uenosono [16]. In their study no conclusion was drawn whether the aspect ratio or grain diameter is the dominant parameter in controlling fracture toughness.

Kawashima et al. [14] and Mitomo [17] showed that the fracture toughness of silicon nitride depends on the diameter of the larger elongated grains. Becher et al. [18] presented a model which relates the fracture toughness to the diameter of the bridging grains according to following equation:

$$K_{IC} = \left\{ (\sigma_r)^2 d_w f \gamma_r E_c / 24 E_r \gamma_i \right\}^{1/2} \quad (2)$$

where  $\sigma_r$  is the tensile strength of the elongated grain,  $d_w$  is the diameter of the elongated grains,  $f$  is the volume fraction of the bridging grains,  $\gamma_r$  and  $\gamma_i$  are the fracture energy and interfacial debonding energy, respectively.  $E_r$  and  $E_c$  are the Young's moduli of the reinforcing phase and composite, respectively.

In the case of whiskers or elongated grains pullout the resultant toughening contribution is also expressed in terms of grain diameter using equation:

$$K_{IC} = \left\{ (\sigma_r)^3 d_w f \gamma_r E_c / 12 E_r \tau_i \right\}^{1/2} \quad (3)$$

where  $\sigma_r$ ,  $d_w$ ,  $f$ ,  $\gamma_r$ ,  $E_r$  and  $E_c$  have the same meaning as in Eq. (2), and  $\tau_i$  is the shear resistance of the interface. In Eq. (3) the fracture toughness is predicted to increase with whiskers content and whiskers diameter. Kleebe et al. [12] reported a continuous increase of fracture toughness for Si<sub>3</sub>N<sub>4</sub> with grain diameter. However, no relationship was developed which relates toughness to the aspect ratio. Recently, Krstic [7] has developed a model which relates fracture toughness to the aspect ratio of the elongated grains. In addition to aspect ratio, the volume fraction of elongated grains plays equally important role as expressed by the equation [7]:

$$K = K_m (1 - V) + \{ 4E\tau V u / (1 - \nu^2) K_m \} \cdot s \quad (4)$$

The model relates the fracture toughness to the pullout length  $u$ , the sliding friction stress  $\tau$ , the grain aspect ratio  $s$  and the elongated grain volume fraction  $V$ .

In Eq. (4)  $K$  is the stress intensity factor of the system,  $K_m$  is the critical stress intensity factor of the fine grain matrix,  $E$  is the Young's modulus and  $\nu$  is the Poisson's ratio.

This paper presents a systematic study of the effect of elongated  $\beta$ -Si<sub>3</sub>N<sub>4</sub> grain morphology on mechanical properties of silicon nitride ceramics especially fracture toughness and fracture strength. Another goal of the paper is to determine which microstructural feature is the dominant factor which controls toughening mechanisms in Si<sub>3</sub>N<sub>4</sub> ceramics.

## Experimental procedure

High purity, fine  $\alpha$ -Si<sub>3</sub>N<sub>4</sub> powder (Ube Industries E-10) was used as a raw material. Alumina (Alcoa A16-SG) and submicron size Y<sub>2</sub>O<sub>3</sub> (Alpha Aesar) powders were used as sintering aids. Five different compositions have been prepared with different Y<sub>2</sub>O<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> ratio (1, 1.5, 2.33, 3, and 4) but keeping constant amount of oxides (Y<sub>2</sub>O<sub>3</sub> + Al<sub>2</sub>O<sub>3</sub>). Compositions were mixed for 12 h by ball-milling with alumina balls. This intensive milling procedure added 0.4 wt.% Al<sub>2</sub>O<sub>3</sub> through the wear of the balls. Polyethylene glycol (PEG) was used as a binder, and after mechanical and isostatic pressing pressureless sintering was carried out in a graphite resistance furnace at temperatures ranging from 1,700 to 1,820°C for 1 h. The atmosphere in the furnace was the flowing N<sub>2</sub> gas. Four point-flexural strength testing was carried out on a jig with an inner and outer span of 20.00 and 40.00 mm, respectively. The cross-head speed was 0.003 mm/min. Ten samples were tested

for each composition. Fracture toughness measurements were carried out using Vickers's indentation method at loads varying from 20 to 30 kg. The fracture toughness values were calculated using the following equation [19]

$$K_{IC} = 0.016 \cdot \left(\frac{E}{H}\right)^{0.5} \cdot \frac{P}{c^{1.5}} \quad (5)$$

where  $H$  is the hardness,  $E$  is the Young's modulus,  $P$  is the load and  $c$  is the crack length.

The Young's moduli of the samples were measured using an impulse-excitation of vibration technique (Grando-Sonic MK5, J.W Lemmens, INC. St. Louis MO USA) according to ASTM standards C 1259–94.

For microstructural analysis, the samples were first polished and then chemically etched with NaOH at 350°C for 130 s. Optical microscopy was used to examine polished and chemically etched surfaces. Scanning Electron Microscope (SEM) (Model JSM 840, Jeol Ltd., Tokyo, Japan) was employed to study the microstructure with an acceleration voltage of 20 KV. UTHSCSA 3.00 *Image Tool* was used as a software for microstructural analysis. It is based on "Area analysis" in which the volume fraction occupied by a certain phase is approximately equal to the portion of the surface occupied by the same phase in a section surface, provided that the particles are randomly distributed. For each composition section surface has taken from three different directions.

## Results and discussion

The microstructure of sintered  $\text{Si}_3\text{N}_4$  consists of bi-modal grains separated by glassy grain boundary phase. Figures 1, 2 and 3 show the effect of Y/A ( $\text{Y}_2\text{O}_3/\text{Al}_2\text{O}_3$ ) ratio on grain morphology and grain size. For example, elongated grains in the composition Y/A ratio of 2.33 (Fig. 2) have the highest aspect ratio of  $\sim 4.92$ , while composition with Y/A ratio of 4 gave the highest width of the grains  $\sim 0.8 \mu\text{m}$  (Fig. 3). The highest density but lowest aspect ratio and width of the grains was observed for composition with Y/A ratio of 1 (Fig. 1). Figures 4 and 5 show the fracture surface of samples with Y/A ratios of 1 and 2.33, respectively. The samples exhibit mostly intergranular fracture with some indication for elongated grain pull-out (see arrows in Figs. 4 and 5).

The effect of average aspect ratio on fracture strength for different Y/A ratios is shown in Fig. 6. Clearly, the addition of  $\text{Y}_2\text{O}_3$  increases the aspect ratio of the  $\text{Si}_3\text{N}_4$  grains reaching the highest value of  $\sim 4.92$  at Y/A ratio of 2.33. Also, according to Fig. 6 any increase in average aspect ratio leads to an increase in strength of  $\text{Si}_3\text{N}_4$ .

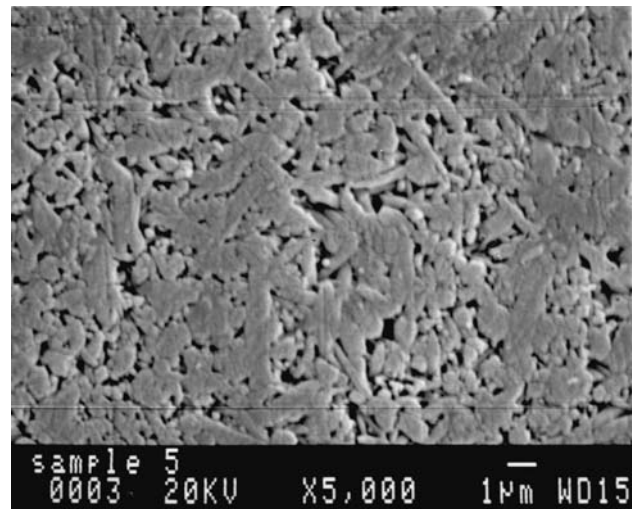


Fig. 1 Microstructure of sample with Y/A ratio of 1

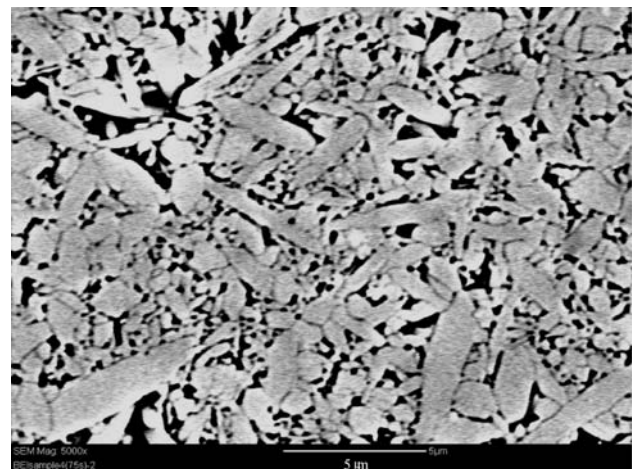


Fig. 2 Microstructure of sample with Y/A ratio of 2.33 (BSE mode)

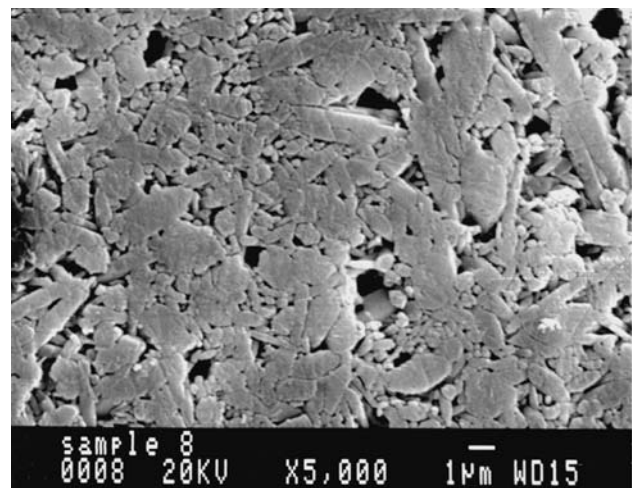
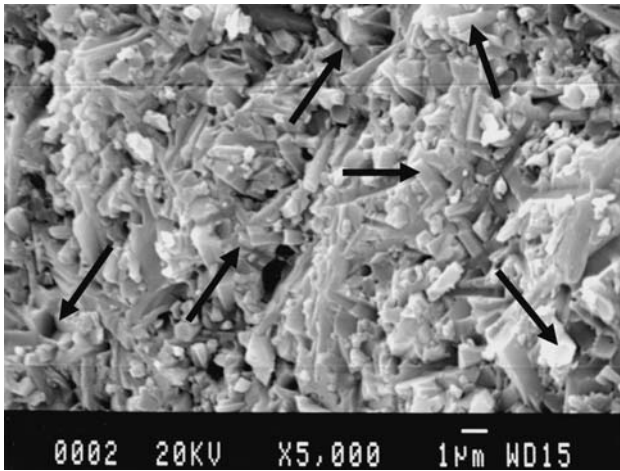
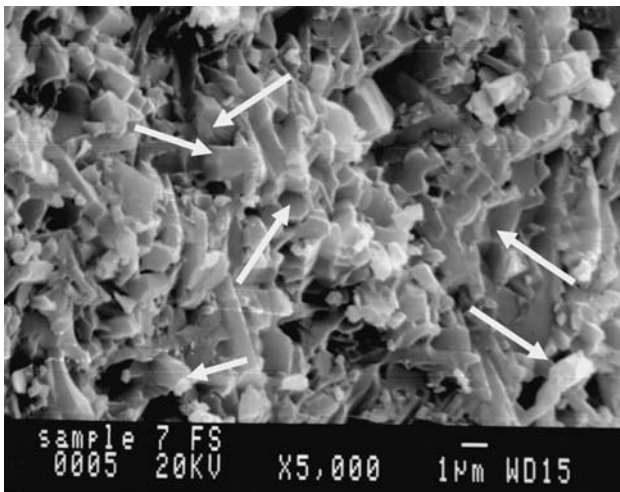


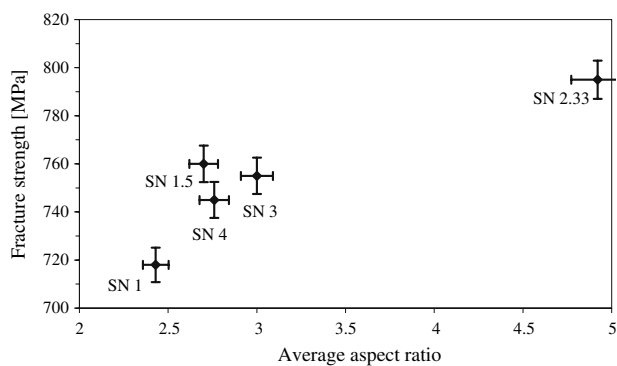
Fig. 3 Microstructure of sample with Y/A ratio of 4



**Fig. 4** Fracture surface of sample with Y/A ratio of 1



**Fig. 5** Fracture surface of sample with Y/A ratio of 2.33



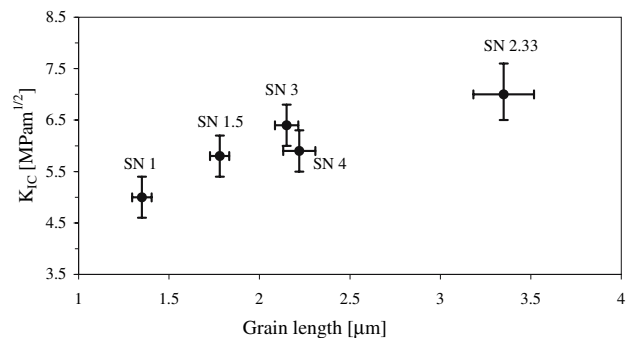
**Fig. 6** Effect of average aspect ratio on strength for Y/A ratios

However, as the aspect ratio is increased there is an increase in the level of porosity (Ins. of Figs. 1–3), which in turn leads to a decrease in strength as shown in Fig. 6. Based on Figs. 1–3 and 6 the dominant mechanism of

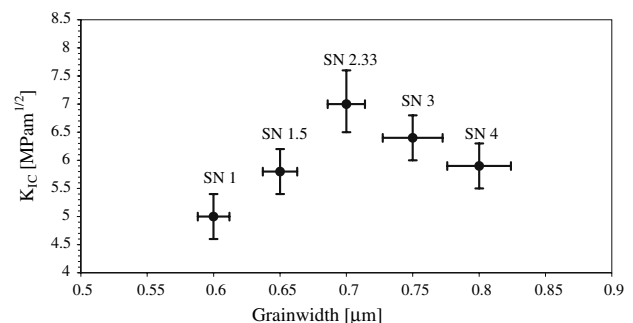
strengthening for samples with Y/A ratio of  $\leq 2.33$  is crack bridging by the elongated  $\beta$ - $\text{Si}_3\text{N}_4$  grains and associated crack deflection. However, for Y/A ratios  $> 2.33$  the dominant factor controlling the strength is porosity.

For fracture toughness determination, both the grain width and grain length were measured. Figures 7 and 8 show the change of fracture toughness with length and width of the grains, respectively. A continuous increase in fracture toughness with length of the grain is observed for all Y/A ratios. According to the Fig. 7 the highest fracture toughness was observed in samples with highest grain length. However, different relationship was found for the effect of grain width on the fracture toughness as shown in Fig. 8.

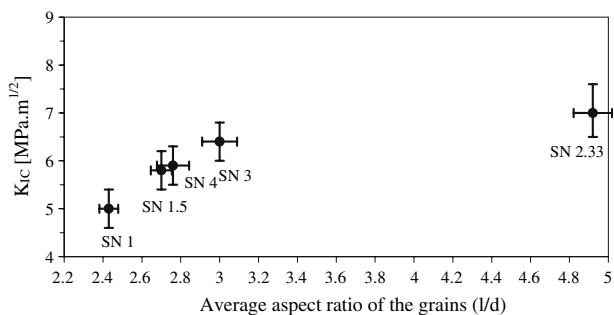
Figure 8 shows that the largest width of the grain does not coincide with the highest fracture toughness suggesting that the grain width alone does not control the fracture toughness. The highest width of the grains (i.e.  $0.8 \mu\text{m}$ ), is found for Y/A ratio of 4, which is not the composition with the highest fracture toughness. The lowest width of the grains of  $0.6 \mu\text{m}$  was found in samples with Y/A ratio of 1 and this sample exhibits the lowest fracture toughness. This behavior is in agreement with Eq. (4) which predicts that the grain aspect ratio is the key factor which controls the toughening and not the grain width alone. In order to test



**Fig. 7** Effect of average grain length on the fracture toughness for different Y/A ratios



**Fig. 8** Effect of average grain width on the fracture toughness for different Y/A ratios



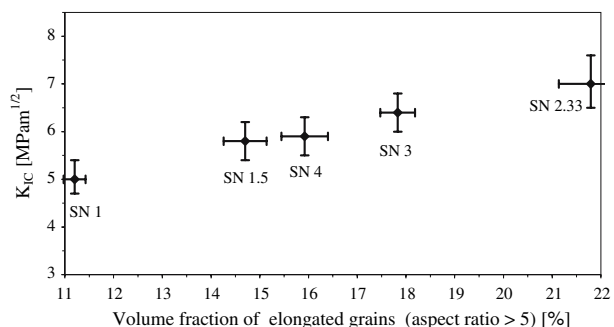
**Fig. 9** Effect of average aspect ratio on the fracture toughness for different Y/A ratios

this prediction, a graph showing the change of  $K_{IC}$  as a function of aspect ratio was produced and presented in Fig. 9.

Although the relationship between fracture toughness and grain aspect ratio is not linear as predicted in Eq. (4), it does show that the aspect ratio controls the fracture toughness.

In developing the relationship between fracture toughness and grain aspect ratio in Fig. 9, the measurements were done only on grains with aspect ratios above ~1, without regard for the number or volume fraction of such grains. In order to determine the exact role of elongated grain volume fraction in toughening, the experimental measurements were done on samples with various Y/A ratios and the volume fraction was determined for grains with aspect ratio of over 5. This is an average aspect ratio between the smallest (~1) and largest (~11) elongated grain aspect ratios found in all samples. The results are presented in Fig. 10.

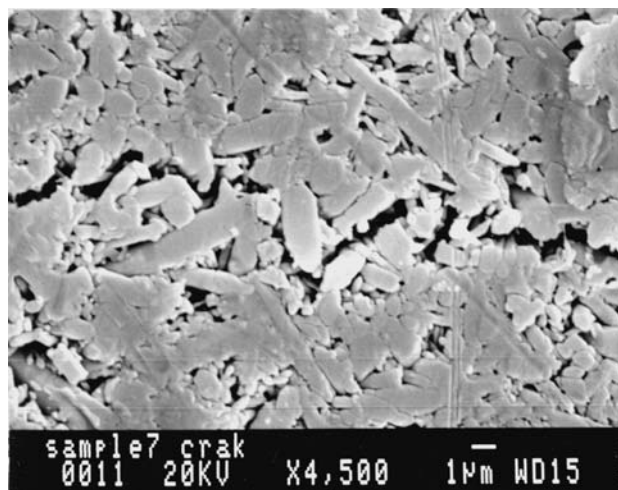
Figure 10 shows that the fracture toughness increases continuously with increasing of volume fraction of elongated grains. The highest value for toughness is found for volume fraction of elongated grains of ~22%, which is approximately one-third of the total elongated grains in the



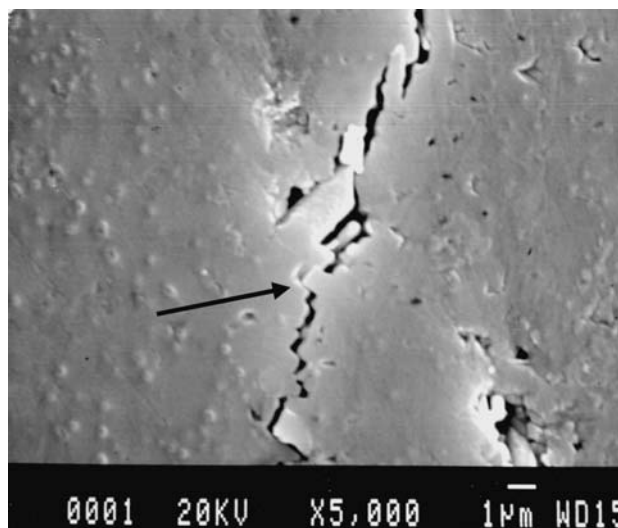
**Fig. 10** Effect of the volume fraction of the elongated grains on the fracture toughness

microstructure (all grains with aspect ratio of >1). This high volume fraction of grains with aspect ratio of >5 is found in samples containing higher amount of  $Y_2O_3$  which confirms once again that yttria plays a critical role in enhancing the growth of elongated  $\beta-Si_3N_4$  grains and thus in toughening.

The two strengthening and toughening mechanisms that operate most effectively in this system with elongated grains of high aspect ratio are crack deflection shown in Fig. 11 and crack bridging and pull-out shown in Fig. 12. One important conclusion that can be inferred from Figs. 6 and 9 is that both strength and toughness exhibit identical dependence on aspect ratio which indicates that the same mechanisms (Figs. 11 and 12) are responsible for both strengthening and toughening.



**Fig. 11** Crack deflection in sample with Y/A ratio of 2.33



**Fig. 12** Crack bridging and pull-out

## Conclusion

It has been shown that the aspect ratio of the elongated grains plays the most important role in strengthening and toughening of  $\text{Si}_3\text{N}_4$  ceramics. The maximum values for fracture toughness of  $7 \text{ MPam}^{1/2}$  and strength 800 MPa, were obtained at the same Y/A ratio (2.33) suggesting that the same toughening mechanism(s) controls both the toughness and strength.

The microstructure of the sintered compacts consists mostly of  $\beta\text{-Si}_3\text{N}_4$  elongated grains, with average aspect ratios between 2.35 and 4.92 uniformly distributed in the matrix of equiaxed or slightly elongated grains, separated by continuous oxide phases at the grain boundaries. Pores are located mainly within the oxide phase at the junction regions of the  $\text{Si}_3\text{N}_4$  grains. Control of microstructure in  $\text{Si}_3\text{N}_4$  is found to be a powerful method of imparting high fracture toughness and strength. The desirable microstructure that can offer high resistance to crack propagation is the one consisting of elongated grains in a matrix of equiaxed grains. The fracture toughness and strength of  $\text{Si}_3\text{N}_4$  ceramics are controlled by the  $\beta\text{-Si}_3\text{N}_4$  grain morphology and aspect ratio.

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